#### The Long-term Decline of the U.S. Job Ladder

#### Aniket Baksy

#### Daniele Caratelli

Digit Research Centre University of Sussex Office of Financial Research U.S. Department of Treasury Niklas Engbom NYU Stern CEPR, NBER, & UCLS



The views expressed are our own and do not necessarily reflect those of the OFR or the Department of Treasury.

### Outline

#### Introduction

Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

# Motivation: why EE mobility matters

**EE** mobility: employer-to-employer moves w/out intervening nonemployment spell

# Motivation: why EE mobility matters

- EE mobility: employer-to-employer moves w/out intervening nonemployment spell
- EE mobility is integral for:
  - 1. Micro: life-cycle wage growth
  - 2. Macro: alleviating misallocation

(Topel and Ward, '92)

(Bilal et al. '22)

# Motivation: why EE mobility matters

- EE mobility: employer-to-employer moves w/out intervening nonemployment spell
- EE mobility is integral for:
  - 1. Micro: life-cycle wage growth (Topel and Ward, '92)
  - 2. Macro: alleviating misallocation

- (Bilal et al. '22)
- Yet little is known about long run trends in EE mobility in the U.S.
  - Empirical: No data before 1994, data post 1994 have issues \*
  - \* Conceptual: Want to isolate mobility **up** the job ladder

#### What we do Literature

1. Propose a method to estimate EE mobility towards higher paying jobs

- \* Inferred through lens of prototypical partial equilibrium job-ladder model
- \* Using publicly available data from the CPS since 1979

#### What we do Literature

- 1. Propose a method to estimate EE mobility towards higher paying jobs
  - \* Inferred through lens of prototypical partial equilibrium job-ladder model
  - \* Using publicly available data from the CPS since 1979
- 2. Establish 3 facts about EE mobility over past half century
  - 1. Fell by more than half since 1979
  - 2. Driven largely by a lower offer arrival rate for employed workers
  - 3. More pronounced for women, less educated, and young workers

#### What we do . Literature

- 1. Propose a method to estimate EE mobility towards higher paying jobs
  - \* Inferred through lens of prototypical partial equilibrium job-ladder model
  - \* Using publicly available data from the CPS since 1979
- 2. Establish 3 facts about EE mobility over past half century
  - 1. Fell by more than half since 1979
  - 2. Driven largely by a lower offer arrival rate for employed workers
  - 3. More pronounced for women, less educated, and young workers
- 3. Evaluate 3 hypotheses behind this decline
  - \* Are workers better matched on average today?
  - \* Decline in matching efficiency?
  - \* Increased labor market concentration?

#### What we do . Literature

- 1. Propose a method to estimate EE mobility towards higher paying jobs
  - \* Inferred through lens of prototypical partial equilibrium job-ladder model
  - \* Using publicly available data from the CPS since 1979
- 2. Establish 3 facts about EE mobility over past half century
  - 1. Fell by more than half since 1979
  - 2. Driven largely by a lower offer arrival rate for employed workers
  - 3. More pronounced for women, less educated, and young workers
- 3. Evaluate 3 hypotheses behind this decline
  - \* Are workers better matched on average today? Unlikely
  - \* Decline in matching efficiency? Unlikely
  - \* Increased labor market concentration? May account for 50% of decline

### Outline

#### Introduction

#### Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

# A partial equilibrium job ladder model

Simple Accounting Framework

- Unit mass of risk-neutral, infinitely lived workers
- Mass  $n_t = 1 e_t$  of nonemployed:

► Mass *e*<sup>*t*</sup> of employed:

## A partial equilibrium job ladder model

Simple Accounting Framework

- Unit mass of risk-neutral, infinitely lived workers
- Mass  $n_t = 1 e_t$  of nonemployed:
  - \* get job offer with prob.  $\lambda_t^n$
  - \* draw from *exogenous* wage offer cdf  $F_{t+1}^n(w)$  (pdf  $f_{t+1}^n(w)$ )
  - \* assume all offers are accepted
- ► Mass *e*<sup>*t*</sup> of employed:

# A partial equilibrium job ladder model

- Unit mass of risk-neutral, infinitely lived workers
- Mass  $n_t = 1 e_t$  of nonemployed:
  - \* get job offer with prob.  $\lambda_t^n$
  - \* draw from exogenous wage offer cdf  $F_{t+1}^n(w)$  (pdf  $f_{t+1}^n(w)$ )
  - \* assume all offers are accepted
- Mass  $e_t$  of employed:
  - \* paid a wage w for as long as they are employed
  - \* lose job with prob.  $\delta_t$
  - \* get job offer with prob.  $\lambda^e_t$
  - \* draw from exogenous wage offer distribution  $F_{t+1}^{e}(w)$  (pdf  $f_{t+1}^{e}(w)$ )
  - \* only accept offers that pay a higher wage

- Let  $g_t(w)$  = share of workers earning wage w and  $G_t(w)$  be the cdf.
- ▶ The mass of workers earning w is  $g_t(w)e_t$ , which evolves according to

$$g_{t+1}(w)e_{t+1} - g_t(w)e_t =$$

- Let  $g_t(w)$  = share of workers earning wage w and  $G_t(w)$  be the cdf.
- ▶ The mass of workers earning w is  $g_t(w)e_t$ , which evolves according to

$$g_{t+1}(w)e_{t+1} - g_t(w)e_t = \underbrace{\lambda_t^n \cdot f_{t+1}^n(w) \cdot n_t}_{t}$$

hires from nonemp.

- Let  $g_t(w)$  = share of workers earning wage w and  $G_t(w)$  be the cdf.
- The mass of workers earning w is  $g_t(w)e_t$ , which evolves according to

$$g_{t+1}(w)e_{t+1}-g_t(w)e_t = \underbrace{\lambda_t^n \cdot f_{t+1}^n(w) \cdot n_t}_{w}$$

hires from nonemp.

$$-\underbrace{\delta_t \cdot g_t(w) \cdot e_t}$$

separations to nonemp.

- Let  $g_t(w)$  = share of workers earning wage w and  $G_t(w)$  be the cdf.
- The mass of workers earning w is  $g_t(w)e_t$ , which evolves according to

$$g_{t+1}(w)e_{t+1} - g_t(w)e_t = \underbrace{\lambda_t^n \cdot f_{t+1}^n(w) \cdot n_t}_{w}$$

hires from nonemp.

$$-\underbrace{\delta_t \cdot g_t(w) \cdot e_t}$$

separations to nonemp.

+ 
$$\lambda_t^e \cdot f_{t+1}^e(w) \cdot G_t(w)e_t$$
  
EE poaching hires

- Let  $g_t(w)$  = share of workers earning wage w and  $G_t(w)$  be the cdf.
- ▶ The mass of workers earning w is  $g_t(w)e_t$ , which evolves according to

$$g_{t+1}(w)e_{t+1} - g_t(w)e_t = \underbrace{\lambda_t^n \cdot f_{t+1}^n(w) \cdot n_t}_{w}$$

hires from nonemp.

$$-\underbrace{\delta_t \cdot g_t(w) \cdot e_t}$$

separations to nonemp.

$$+ \underbrace{\lambda_t^e \cdot f_{t+1}^e(w) \cdot G_t(w)e_t}_{-}$$

EE poaching hires

$$-\underbrace{\lambda_t^e \cdot (1 - F_{t+1}^e(w)) \cdot g_t(w)e_t}_{\text{EE poaching separations}}$$

# Deriving EE mobility

▶ Integrating (1) and rearranging



# Deriving EE mobility

Integrating (1) and rearranging



EE mobility is



# Deriving EE mobility

Integrating (1) and rearranging



EE mobility is



► Recover EE given  $G_t$ ,  $G_{t+1}$ ,  $F_{t+1}^n$ ,  $e_t$ ,  $e_{t+1}$ ,  $\delta_t$ ,  $\lambda_t^n$ , no need to observe  $F_{t+1}^e(w)$ 

### Outline

Introduction

Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

# Data: The Current Population Survey (CPS), 1979-2023

- $\blacktriangleright\,$  Survey of  $\approx\,$  60,000 US households conducted by Census Bureau for BLS
- "4-8-4" rotation pattern



- ▶ Month-to-month changes in employment status → Pin down  $e_t$ ,  $e_{t+1}$ ,  $\lambda_t^n$ ,  $\delta_t$
- ▶  $\approx 25\%$  ("outgoing rotation groups") report earnings → wage distbns G, F → Details

▶ In SS, employment in and outflows equal  $(\delta_t e_t = \lambda_t^n (1 - e_t))$ 

$$\Rightarrow$$
 Can show that  $EE_t = \delta_t \int_{-\infty}^{\infty} \frac{F_{t+1}^n(w) - G_t(w)}{G_t(w)} dG_t(w)$ 

► In SS, employment in and outflows equal  $(\delta_t e_t = \lambda_t^n (1 - e_t))$ 

$$\Rightarrow$$
 Can show that  $EE_t = \delta_t \int_{-\infty}^{\infty} rac{F_{t+1}^n(w) - G_t(w)}{G_t(w)} dG_t(w)$ 

► EE mobility identified by gap  $\equiv F_{t+1}^n(w) - G_t(w)$ 



- ► In SS, employment in and outflows equal  $(\delta_t e_t = \lambda_t^n (1 e_t))$ ⇒ Can show that  $EE_t = \delta_t \int_{-\infty}^{\infty} \frac{F_{t+1}^n(w) - G_t(w)}{G_t(w)} dG_t(w)$
- ► EE mobility identified by gap  $\equiv F_{t+1}^n(w) G_t(w)$



- ► In SS, employment in and outflows equal  $(\delta_t e_t = \lambda_t^n (1 e_t))$ ⇒ Can show that  $EE_t = \delta_t \int_{-\infty}^{\infty} \frac{F_{t+1}^n(w) - G_t(w)}{G_t(w)} dG_t(w)$
- EE mobility identified by gap  $\equiv F_{t+1}^n(w) G_t(w)$  which shrinks over time



### EE Mobility Up the Job Ladder, 1979-2023



#### Validation

Exercise 1: Compare our series, post '96, vs SIPP



#### Validation

- Exercise 1: Compare our series, post '96, vs SIPP
- Exercise 2: Compare NLSY '79 vs our method applied to the same cohort



▶ FMP

### Outline

Introduction

Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

#### Three Facts on EE mobility

- 1. EE mobility declined by nearly half since 1979
- 2. Driven largely by a lower job finding rate for the employed
- 3. Decline larger for female, lower educated and young workers

#### Three Facts on EE mobility

#### 1. EE mobility declined by nearly half since 1979

2. Driven largely by a lower job finding rate for the employed

3. Decline larger for female, lower educated and young workers

### Fact 1: EE mobility decline since 1979

- EE mobility towards higher-paying jobs declined by half from 1979 to 2023
- Much of the decline occurs in the 1980s/90s



On-the-job Wage Growth

Unobservables

#### Three Facts on EE mobility

- 1. EE mobility declined by nearly half since 1979
- 2. Driven largely by a lower job finding rate for the employed
- 3. Decline larger for female, lower educated and young workers

Fact 2. Driven largely by a lower job finding rate for employed


Fact 2. Driven largely by a lower job finding rate for employed



#### Three Facts on EE mobility

- 1. EE mobility declined by nearly half since 1979
- 2. Driven largely by a lower job finding rate for the employed
- 3. Decline larger for female, lower educated and young workers

#### Fact 3: Larger decline for women, less educated, young



t,a,c > cohort

Fact 3: Shift-share exercise (1980-84 to 2014-19)

$$EE_{1} - EE_{0} = \sum_{i \in \mathcal{I}} \left( \underbrace{\left(\omega_{1}^{i} - \omega_{0}^{i}\right) EE_{0}^{i}}_{\text{composition effect}} + \underbrace{\omega_{0}^{i} \left(EE_{1}^{i} - EE_{0}^{i}\right)}_{\text{within-group effect}} + \underbrace{\left(\omega_{1}^{i} - \omega_{0}^{i}\right) \left(EE_{1}^{i} - EE_{0}^{i}\right)}_{\text{covariance}} \right)$$

	Gender	Education	Age	
Composition	-3.3%	11.9%	15.2%	
Within	100.3%	98.5%	98.0%	
Covariance	2.9%	-10.5%	-13.2%	

## Fact 3: Shift-share exercise (1980-84 to 2014-19)

$$EE_{1} - EE_{0} = \sum_{i \in \mathcal{I}} \left( \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) EE_{0}^{i}}_{\text{composition effect}} + \underbrace{\omega_{0}^{i} \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{within-group effect}} + \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{covariance}} \right)$$

	Gender	Education	Age	
Composition	-3.3%	11.9%	15.2%	
Within	100.3%	98.5%	98.0%	
Covariance	2.9%	-10.5%	-13.2%	

Fact 3: Shift-share exercise (1980-84 to 2014-19)

$$EE_{1} - EE_{0} = \sum_{i \in \mathcal{I}} \left( \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) EE_{0}^{i}}_{\text{composition effect}} + \underbrace{\omega_{0}^{i} \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{within-group effect}} + \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{covariance}} \right)$$

	Gender	Education	Age	Age  imes Education
Composition	-3.3%	11.9%	15.2%	28.5%
Within	100.3%	98.5%	98.0%	90.3%
Covariance	2.9%	-10.5%	-13.2%	-18.8%

#### Outline

Introduction

Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

Consider 3 hypotheses consistent with a decline in EE mobility.

- 1. Fall in separation probability
- 2. Better matched workers
- 3. Higher firm labor market concentration

#### Fall in separation probability?

- Higher separation means workers must re-start job ladder climb more often
- In steady state we have



## Fall in separation probability? Unlikely

- Higher separation means workers must re-start job ladder climb more often
- In steady state we have



#### Better matched workers?

Did EE mobility fall because workers are better matched today?

$$EE_{t} = \underbrace{\lambda_{t}^{e}}_{\text{job finding prob.}} \times \underbrace{\int \left(1 - F_{t+1}^{e}(w)\right) dG_{t}(w)}_{\text{acceptance prob.}}$$

#### Better matched workers?

Did EE mobility fall because workers are better matched today?

$$EE_{t} = \underbrace{\lambda_{t}^{e}}_{\text{job finding prob.}} \times \underbrace{\int \left(1 - F_{t+1}^{e}(w)\right) dG_{t}(w)}_{\text{acceptance prob.}}$$

Recall that assuming  $F^e = F^n$ , all EE decline is from job-finding prob.



#### Better matched workers? Unlikely

Did EE mobility fall because workers are better matched today?

$$EE_{t} = \underbrace{\lambda_{t}^{e}}_{\text{job finding prob.}} \times \underbrace{\int \left(1 - F_{t+1}^{e}(w)\right) dG_{t}(w)}_{\text{acceptance prob.}}$$

Recall that assuming  $F^e = F^n$ , all EE decline is from job-finding prob.



## Higher firm labor market concentration

- Did EE mobility fall because of increased firm market concentration?
  - Higher market concentration lowers workers' opportunities to switch employers



 $\Delta EE \text{ vs } \Delta Firms / worker$ 



In panel of states since 1980, we find

► +ve relationship b/n firms/worker &  $\Delta EE$ 

 $\Delta \lambda_e$  vs  $\Delta Firms / worker$ 



In panel of states since 1980, we find

▶ +ve relationship b/n firms/worker &  $\Delta EE$ 

 $\blacktriangleright$  driven largely by  $\Delta \lambda_e$ 

#### $\Delta Acc.$ Prob. vs $\Delta Firms / worker$



In panel of states since 1980, we find

▶ +ve relationship b/n firms/worker &  $\Delta EE$ 

► driven largely by  $\Delta \lambda_e$ 

 $\blacktriangleright$  and not by  $\triangle$  acceptance rate



In panel of states since 1980, we find

- ▶ +ve relationship b/n firms/worker &  $\Delta EE$
- ► driven largely by  $\Delta \lambda_e$
- $\blacktriangleright$  and not by  $\Delta \texttt{acceptance}$  rate
- $\Delta$ firms/worker  $\implies$  over half of  $\downarrow EE$

### Outline

Introduction

Methodology

Data, Estimation and Validation

Three Facts about EE Mobility

Three Hypotheses Regarding Decline

Conclusion

#### Conclusion

▶ We estimate EE mobility halved since 1979 using job-ladder model and public data

- ► As a consequence, associated annual wage growth fell by over 1 p.p.
- Bigger declines for women, non-college educated workers, and newer cohorts
- Framework suggests EE decline:
  - Unlikely to be driven by better matches or worse matching efficiency
  - Consistent with rising labour market concentration

# Thank You!

Appendix

#### Our Method: An Accounting Framework Back

- Let w denote a residualized wage.
- Suppose we observe, between t and t + 1,

•  $G_t(w)$  workers earning less than w at t and  $G_{t+1}(w)$  at t+1





#### Our Method: An Accounting Framework Back

- Let w denote a residualized wage.
- Suppose we observe, between t and t + 1,
  - $G_t(w)$  workers earning less than w at t and  $G_{t+1}(w)$  at t+1
  - ▶  $H_t(w)$  non-employed workers find a job paying at least w

$$\underbrace{G_t(w)}_{\text{earn } \leq w \text{ at } t} + \underbrace{H_t(w)}_{\text{inflows}}$$



#### Our Method: An Accounting Framework

- Let w denote a residualized wage.
- Suppose we observe, between t and t + 1,
  - $G_t(w)$  workers earning less than w at t and  $G_{t+1}(w)$  at t+1
  - ▶  $H_t(w)$  non-employed workers find a job paying at least w
  - $\triangleright$   $S_t(w)$  workers earning at least w at t separate to non-employment



#### Our Method: An Accounting Framework Back

- Let w denote a residualized wage.
- Suppose we observe, between t and t + 1,
  - $G_t(w)$  workers earning less than w at t and  $G_{t+1}(w)$  at t+1
  - ▶  $H_t(w)$  non-employed workers find a job paying at least w
  - ▶  $S_t(w)$  workers earning at least w at t separate to non-employment



 $\implies$  Mass  $x_t(w)$  workers must have moved from  $\leq w$  to above w

#### Our Method: An Accounting Framework - Back

- Let w denote a residualized wage.
- Suppose we observe, between t and t + 1,
  - $G_t(w)$  workers earning less than w at t and  $G_{t+1}(w)$  at t+1
  - ▶  $H_t(w)$  non-employed workers find a job paying at least w
  - $\triangleright$   $S_t(w)$  workers earning at least w at t separate to non-employment

$$\underbrace{\mathcal{G}_t(w)}_{\mathsf{earn} \leq w \; \mathsf{at} \; t} + \underbrace{\mathcal{H}_t(w)}_{\mathsf{inflows}} - \underbrace{\mathcal{S}_t(w)}_{\mathsf{outflows}} + \underbrace{\mathsf{x}_t(w)}_{\mathsf{EE} \; \mathsf{to} \geq w} = \underbrace{\mathcal{G}_{t+1}(w)}_{\mathsf{earn} \leq w \; \mathsf{at} \; t+1}$$

 $\implies$  Mass  $x_t(w)$  workers must have moved from  $\leq w$  to above w

▶ If only source of residual wage growth,  $x_t(w)$  is #EE moves to higher wage!

#### Literature . Back

#### Construct EE transition probability since 1979

Fallick and Fleischman '04; Nagypal '08; Hyatt and Spletzer ('13, '16, '17); Molloy et al. '16; Haltwanger et al. '18; Fujita, Moscarini and Postel-Vinay '23, Molloy, Smith and Wozniak '24

#### Labor market flow balance accounting applied to EE mobility

Jolivet, Postel-Vinay and Robin '06; Elsby, Michaels and Solon '09; Shimer '12

#### Explanations for decline in EE mobility

Molloy et al. '16; Mercan '17; Macaluso, Hershbein and Yeh, '19; Azar et al. '20; Prager and Schmitt '21; Azar, Marinescu and Steinbaum '22; Berger, Herkenhoff and Mongey '22; Handwerker and Dey '22; Pries and Rogerson '22, Rinz '22; Bagga '23

#### Validation: post 1996 · Back



## Allowing on-the-job wage growth

- Allow wages to grow at rate  $\xi$  with tenure
- Small effects: OTJ wage growth much smaller than wage rise after EE move



## On-the-job wage growth rate

- ▶ Allow residual wages to grow at rate  $\xi$  with tenure
- Small effects: OTJ wage growth much smaller than wage rise after EE move

Back



## Controlling for Unobservables

- Observe wages for each individual twice: once in month 4 and once in month 16
- Residualize wages on past wages for same individual



Individual FEs

Back

### Individual Fixed Effects

Observe wages for each individual twice: once in month 4 and once in month 16

Back

 $\implies$  Residualize wages on individual FEs



EE Moves are only source of residual wage growth

Key for identification: EE moves are only source of residual wage growth



Back

#### Time - Age - Cohort Decomposition

#### Back

Decompose  $\Delta EE_t$  into time, age and cohort effects under assumption that age effects are stable between ages 50-59.



#### Time - Age - Cohort Decomposition

#### Back

Decompose  $\Delta EE_t$  into time, age and cohort effects under assumption that age effects are stable between ages 50-59.


Fact 3: Shift-share exercise (1980-84 to 2014-19)

$$EE_{1} - EE_{0} = \sum_{i \in \mathcal{I}} \left( \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) EE_{0}^{i}}_{\text{composition effect}} + \underbrace{\omega_{0}^{i} \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{within-group effect}} + \underbrace{\left( \omega_{1}^{i} - \omega_{0}^{i} \right) \left( EE_{1}^{i} - EE_{0}^{i} \right)}_{\text{covariance}} \right)$$

	Gender	Race	Education	Age	$Age{\times}Education$
Composition	-3.3%	-1.6%	11.9%	15.2%	28.5%
Within	100.3%	100.4%	98.5%	98.0%	90.3%
Covariance	2.9%	1.1%	-10.5%	-13.2%	-18.8%
Total	100%	100%	100%	100%	100%

Back

## Within-state changes, 1980s-2010s

Back

	(1) EE	$(2) \\ \Delta w$	(3) λ <sup>e</sup>	$\begin{array}{c} (4) \\ \lambda^n \end{array}$
Firms per worker	1.793*** (0.556)	0.094 (0.239)	1.699*** (0.554)	-0.063 (0.102)
Emp. Share of Large Firms $(\geq 1000 \text{ emp.})$	-1.535*** (0.414)	-0.160 (0.205)	-1.375*** (0.443)	-0.231 (0.136)
Emp. Share of Small Firms (< 100 emp.)	2.009*** (0.675)	0.109 (0.230)	1.900*** (0.675)	0.161 (0.151)

 $y_{st} = \beta imes Conc_{st} + \xi_s + \phi_t + \varepsilon_{st}$ 

- Sample: individuals aged 16+, non-missing demo. info, residing in 50 states + DC
- Link individuals across months using validated longitudinal identifiers (cpsidv)
- ▶ Wages = usual earnings/week divided by usual hours worked/week, deflate by CPI
  - ▶ Residual wages: predicted values from running  $w_{i,t} = \xi_{a,r,g,e,y} + \xi_{s,t} + \varepsilon_{i,t}$
  - winsorize top/bottom 0.5%, group into 100 bins (robust to #bins)

## Data Details

## Back

Estimate offer distribution using weighted shares of workers hired from non-employment in each wage bin

$$f_{t,i}^{n} = \frac{1}{dw_{i}} \frac{\sum_{j} \mathbb{1}_{b_{i-1} \leq \widehat{w}_{t,j} < b_{i}} * \mathbb{1}_{hire_{t,j}^{n} = 1} * weight_{t,j}}{\sum_{j} \mathbb{1}_{hire_{t,j}^{n} = 1} * weight_{t,j}}$$
(1)

Estimate wage distribution using weighted shares of all employed workers in each wage bin

$$g_{t,i} = \frac{1}{dw_i} \frac{\sum_j \mathbb{1}_{b_{i-1} \le \widehat{w}_{t,j} < b_i} * weight_{t,j}}{\sum_j weight_{t,j}}$$
(2)